

ROBOTICS &  
PERCEPTION  
GROUP



University of  
Zurich<sup>UZH</sup>

# Visual-Inertial Localization and Mapping for Robot Navigation

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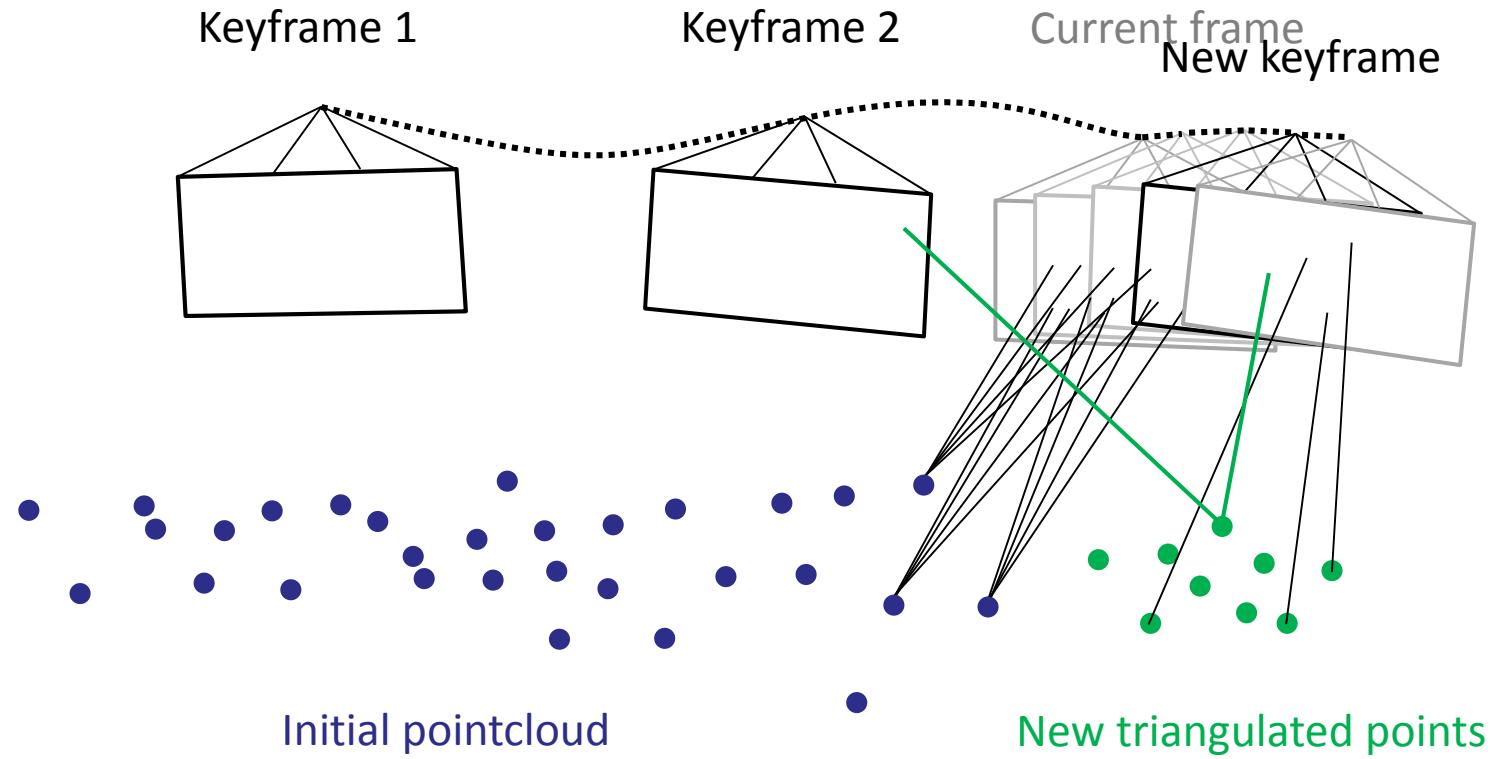
# Mocular,Vision-inertial Navigation of Mobile Robots

<https://www.youtube.com/watch?v=vHpw8zc7-JQ>



[Scaramuzza, Achterlik, Weiss, Fraundorfer, et al., Vision-Controlled Micro Flying Robots: from System Design to Autonomous Navigation and Mapping in GPS-denied Environments, IEEE RAM, 2014]

# Keyframe-based Visual Odometry



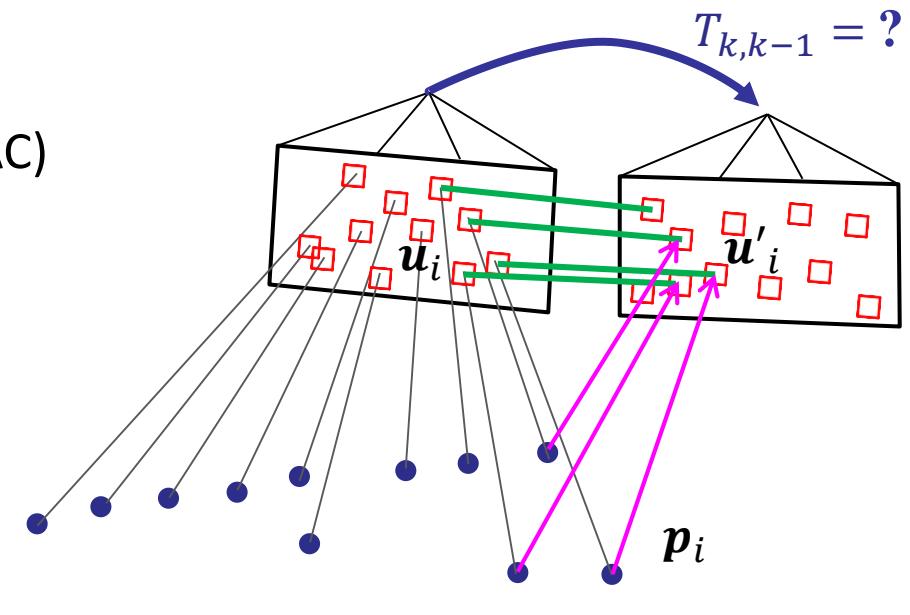
PTAM (Parallel Tracking & Mapping) [Klein, ISMAR'08]

# Feature-based methods

1. Extract & match features (+RANSAC)

2. Minimize **Reprojection error**  
minimization

$$T_{k,k-1} = \arg \min_T \sum_i \| \mathbf{u}'_i - \pi(\mathbf{p}_i) \|_{\Sigma}^2$$

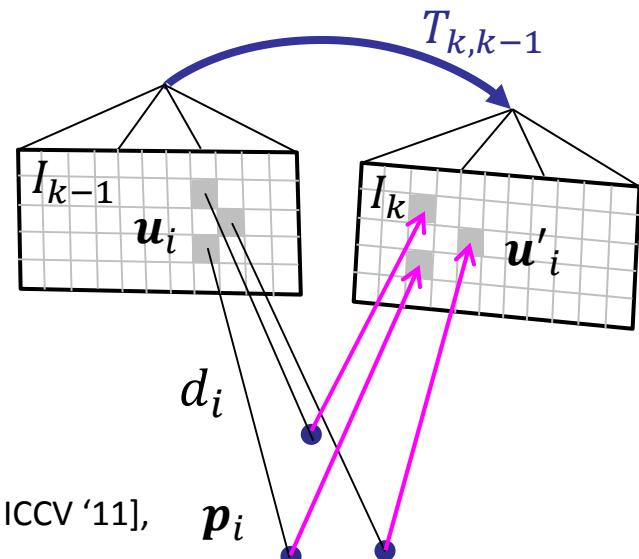


# Direct methods

1. Minimize **photometric error**

$$T_{k,k-1} = \arg \min_T \sum_i \| I_k(\mathbf{u}'_i) - I_{k-1}(\mathbf{u}_i) \|_{\sigma}^2$$

where  $\mathbf{u}'_i = \pi(T \cdot (\pi^{-1}(\mathbf{u}_i) \cdot d))$



[Jin,Favaro,Soatto'03] [Silveira, Malis, Rives, TRO'08], [Newcombe et al., ICCV '11],  
[Engel et al., ECCV'14], [Forster et al., ICRA'14]

# Feature-based methods

1. Extract & match features (+RANSAC)
2. Minimize **Reprojection error** minimization

- ✓ Large frame-to-frame motions
- ✗ Slow due to costly feature extraction and matching
- ✗ Matching Outliers (RANSAC)

$$T_{k,k-1} = \arg \min_T \sum_i \| \mathbf{u}'_i - \pi(\mathbf{p}_i) \|_{\Sigma}^2$$

## Direct methods

1. Minimize photometric error

$$T_{k,k-1} = \arg \min_T \sum_i \| I_k(\mathbf{u}'_i) - I_{k-1}(\mathbf{u}_i) \|_{\sigma}^2$$

where  $\mathbf{u}'_i = \pi(T \cdot (\pi^{-1}(\mathbf{u}_i) \cdot d))$

- ✓ All information in the image can be exploited (precision, robustness)
- ✓ Increasing camera frame-rate reduces computational cost per frame
- ✗ Limited frame-to-frame motion

# Feature-based methods

1. Extract & match features (+RANSAC)
2. Minimize **Reprojection error** minimization

- ✓ Large frame-to-frame motions
- ✗ Slow due to costly feature extraction and matching

Our solution:

## SVO: *Semi-direct Visual Odometry* [ICRA'14]

Combines feature-based and direct methods

$$T_{k,k-1} = \arg \min_T \sum_i \| \iota_k(\mathbf{u}_i) - \iota_{k-1}(\mathbf{u}_i) \| \sigma$$

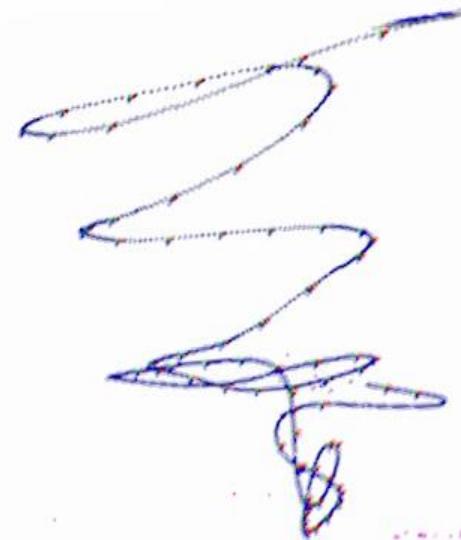
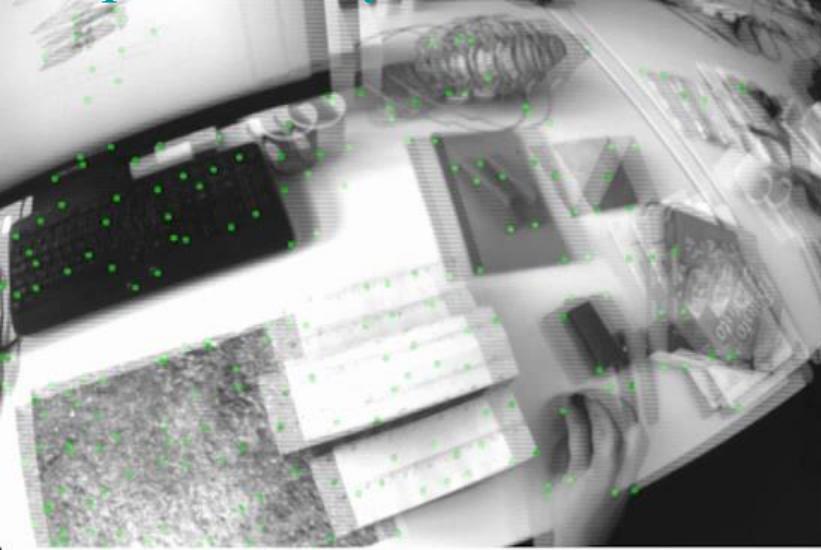
frame

where  $\mathbf{u}'_i = \pi(T \cdot (\pi^{-1}(\mathbf{u}_i) \cdot d))$

- ✗ Limited frame-to-frame motion

# SVO Results: Fast and Abrupt Motions

<https://www.youtube.com/watch?v=2YnIMfw6bJY>



Open Source

[Forster, Pizzoli, Scaramuzza, «SVO: Semi Direct Visual Odometry», ICRA'14]

# Processing Times of SVO

Laptop (Intel i7, 2.8 GHz)

400 frames per second



Embedded ARM Cortex-A9, 1.7 GHz

Up to 70 frames per second



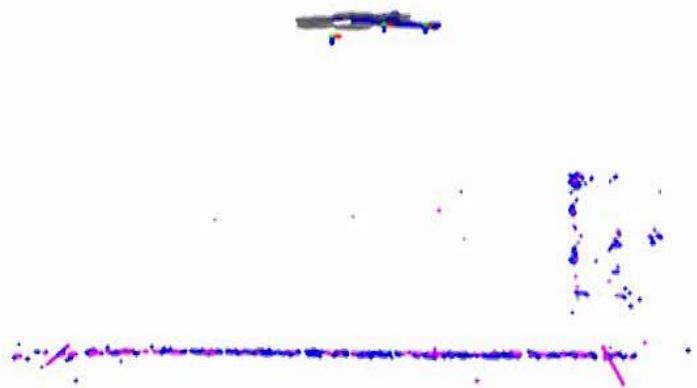
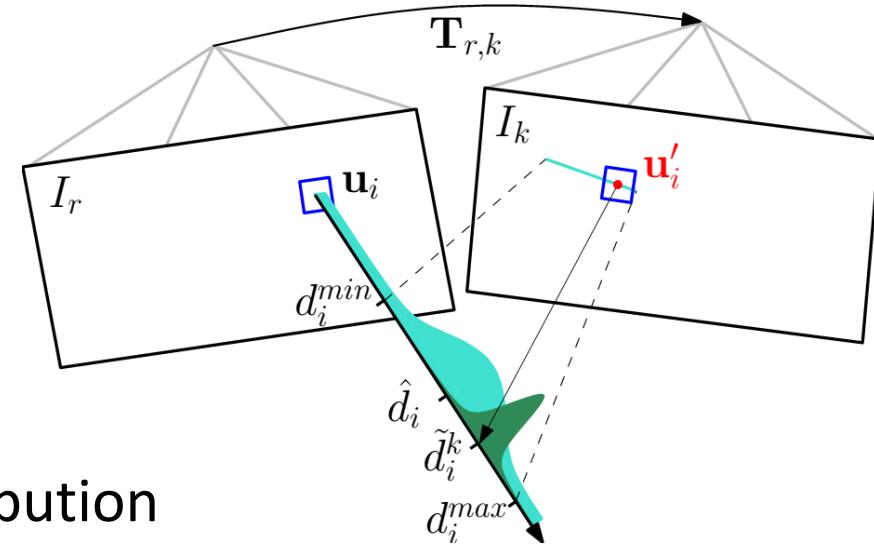
# Probabilistic Depth Estimation

Depth-Filter:

- **Depth Filter** for every feature
- **Recursive Bayesian** depth estimation

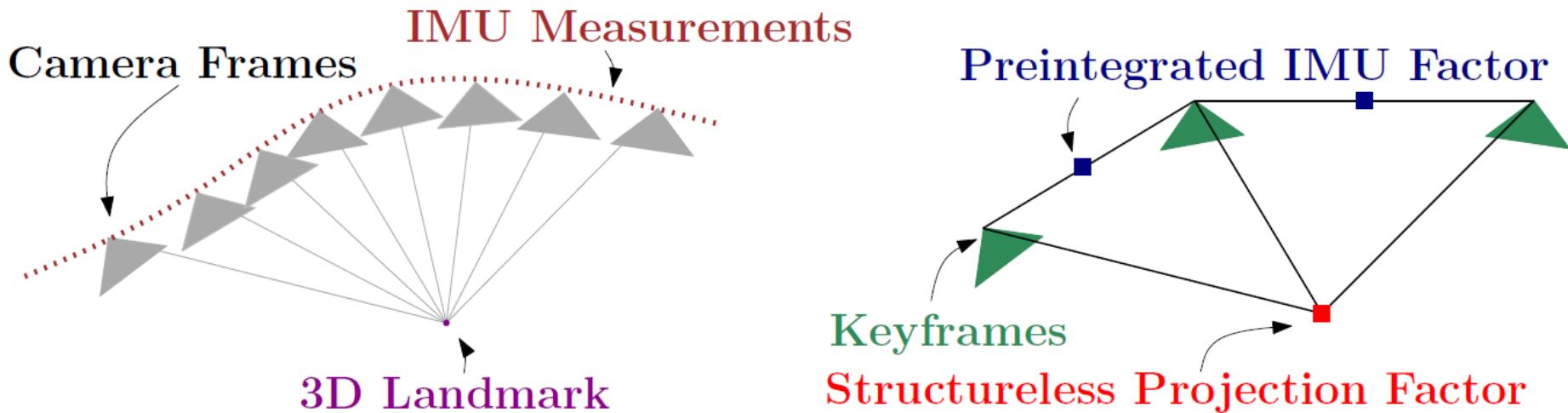
Mixture of Gaussian + Uniform distribution

$$p(\tilde{d}_i^k | d_i, \rho_i) = \rho_i \mathcal{N}(\tilde{d}_i^k | d_i, \tau_i^2) + (1 - \rho_i) \mathcal{U}(\tilde{d}_i^k | d_i^{\min}, d_i^{\max})$$



# Visual-Inertial Fusion via Optimization [RSS'15]

- Fusion solved as a *non-linear optimization problem* (no Kalman filter):
- Increased accuracy over filtering methods



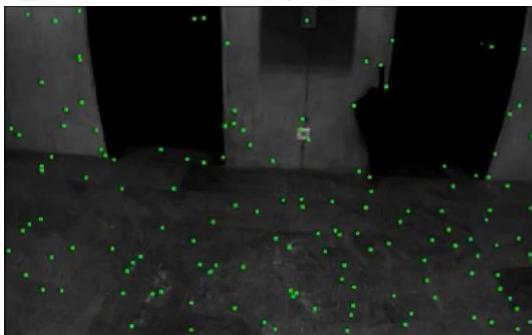
$$\sum_{(i,j) \in \mathcal{K}_k} \|\mathbf{r}_{\mathcal{I}_{ij}}\|_{\Sigma_{ij}}^2 + \sum_{i \in \mathcal{K}_k} \sum_{l \in \mathcal{C}_i} \|\mathbf{r}_{\mathcal{C}_{il}}\|_{\Sigma_c}^2$$

*IMU residuals*      *Reprojection residuals*

# Comparison with Previous Works

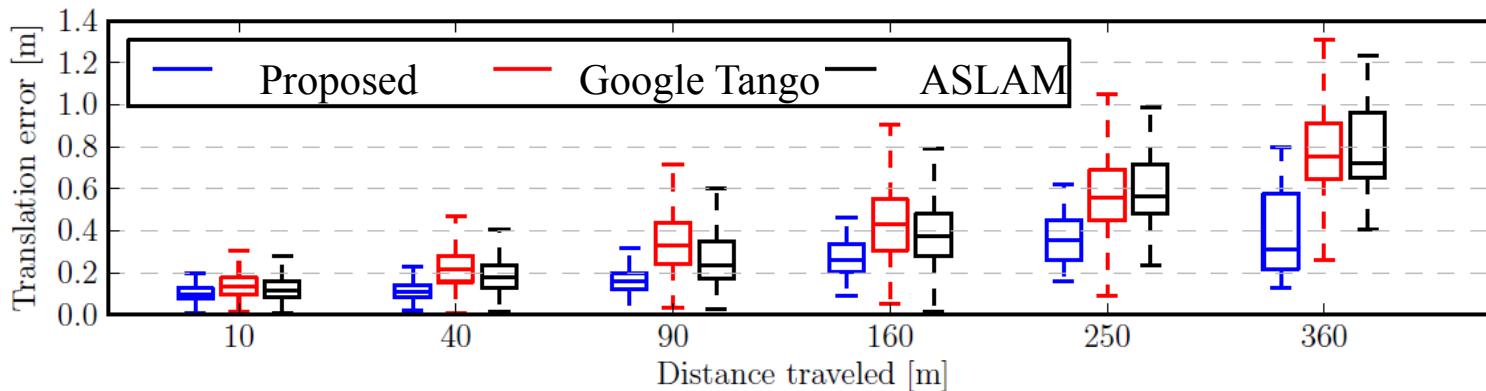
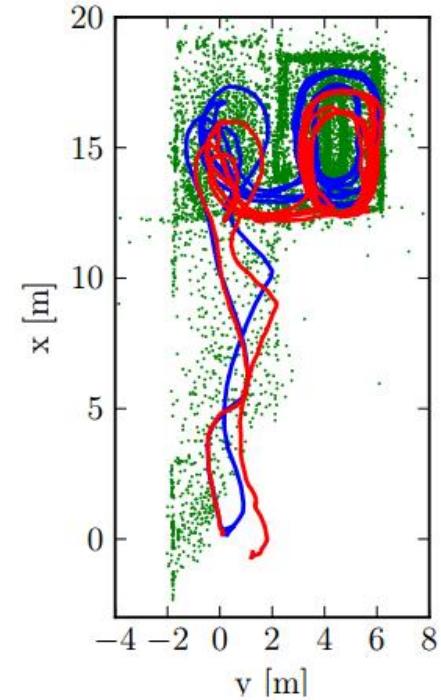
<https://www.youtube.com/watch?v=Csjkci5lfco>

Open Source



5x

Accuracy: 0.1% of the travel distance

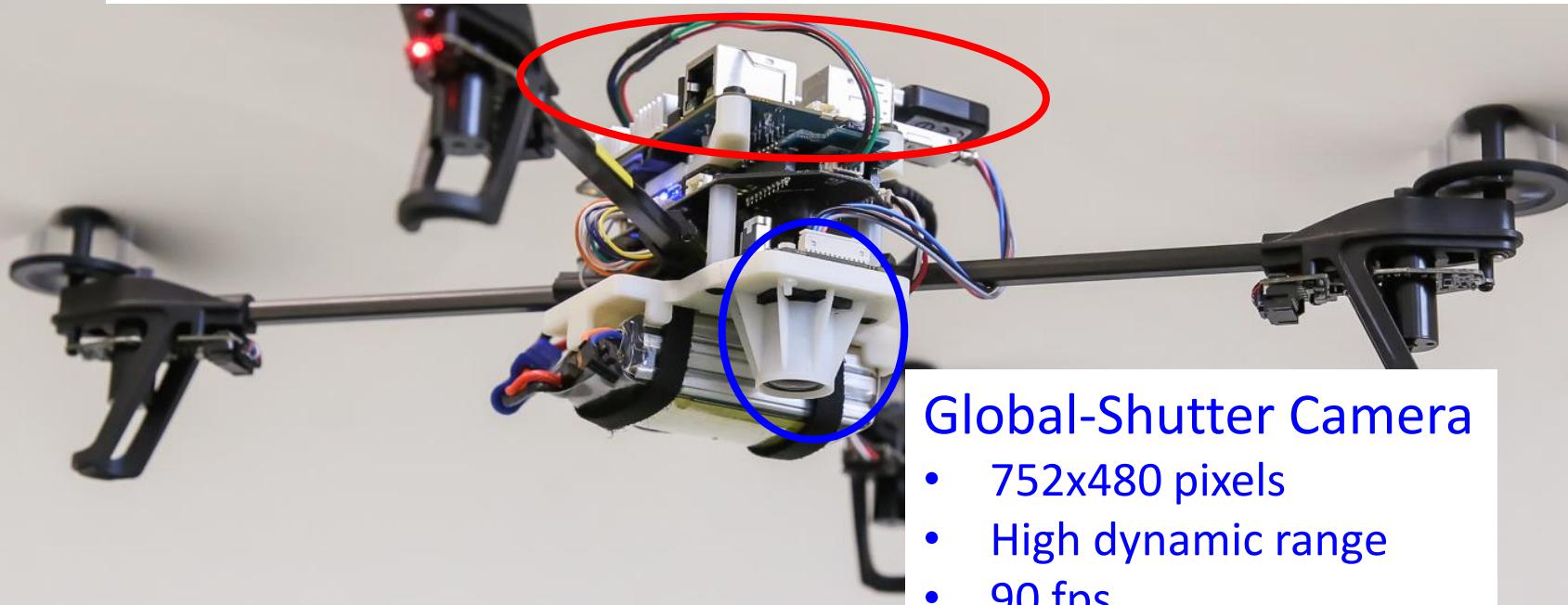


# Integration on a Quadrotor Platform

# Quadrotor System

## Odroid U3 Computer

- Quad Core Odroid (ARM Cortex A-9) used in Samsung Galaxy S4 phones
- Runs Linux Ubuntu and ROS



## Global-Shutter Camera

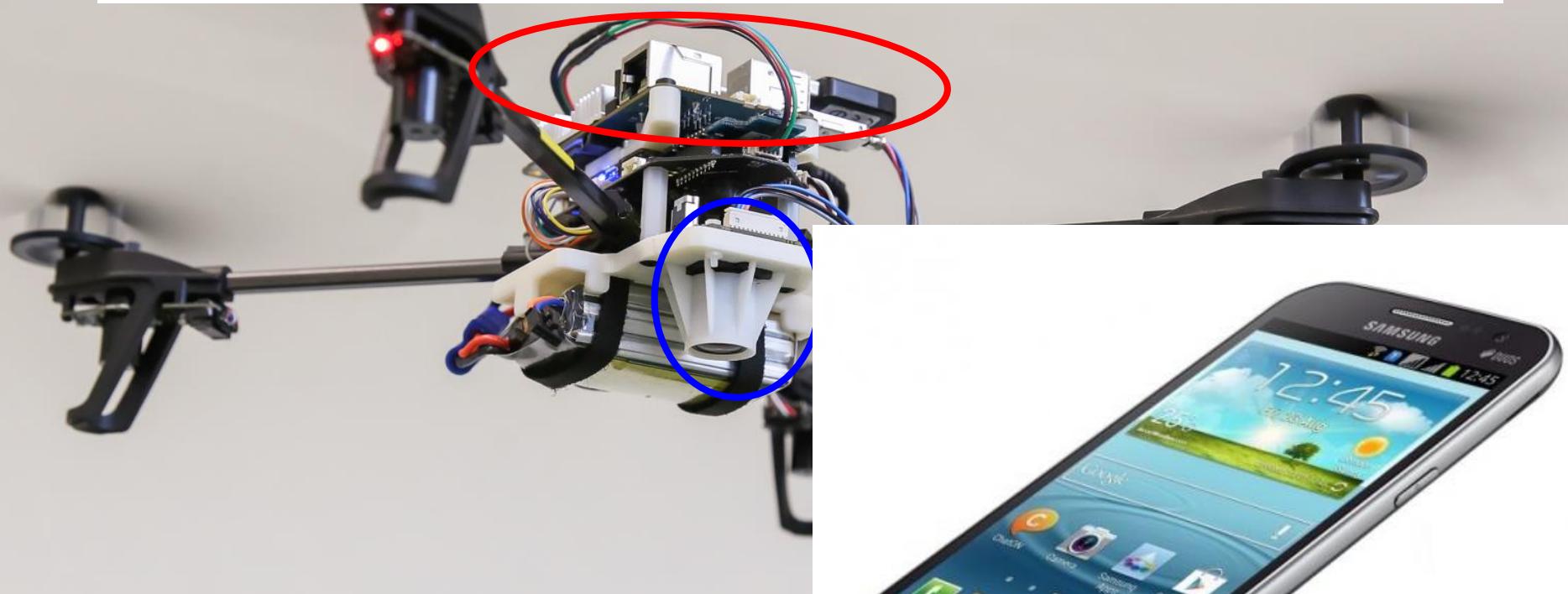
- 752x480 pixels
- High dynamic range
- 90 fps

450 grams

# Quadrotor System

## Odroid U3 Computer

- Quad Core Odroid (ARM Cortex A-9) used in Samsung Galaxy S4 phones
- Runs Linux Ubuntu and ROS



450 grams

# Indoors and outdoors experiments

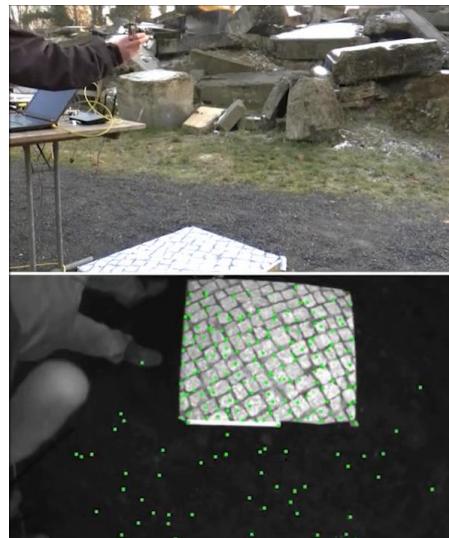
[https://www.youtube.com/watch?v=4X6Voft4Z\\_0](https://www.youtube.com/watch?v=4X6Voft4Z_0)



RMS error: 5 mm, height: 1.5 m – Down-looking camera



Speed: 4 m/s, height: 1.5 m – Down-looking camera



<https://www.youtube.com/watch?v=3mNY9-DSUDk>

3x

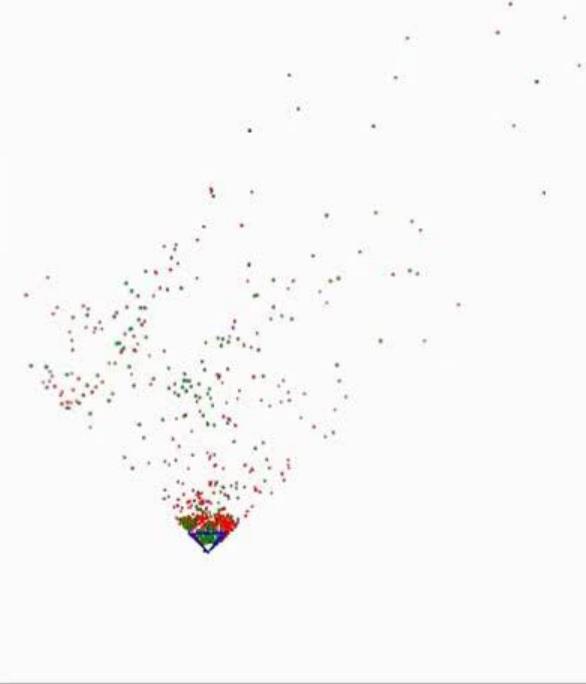


Faessler, Fontana, Forster, Mueggler, Pizzoli, Scaramuzza, Autonomous, Vision-based Flight and Live Dense 3D Mapping with a Quadrotor Micro Aerial Vehicle, **Journal of Field Robotics**, 2015.

# Visual-Inertial Odometry - Results

<https://www.youtube.com/watch?v=6KXBoprGaR0>

SVO with a single camera on Euroc dataset



**Open Source**

# Application: Autonomous Inspection of Bridges and Power Masts

Project with Parrot: Autonomous vision-based navigation

<https://www.youtube.com/watch?v=BxVoaLrKJ4U>



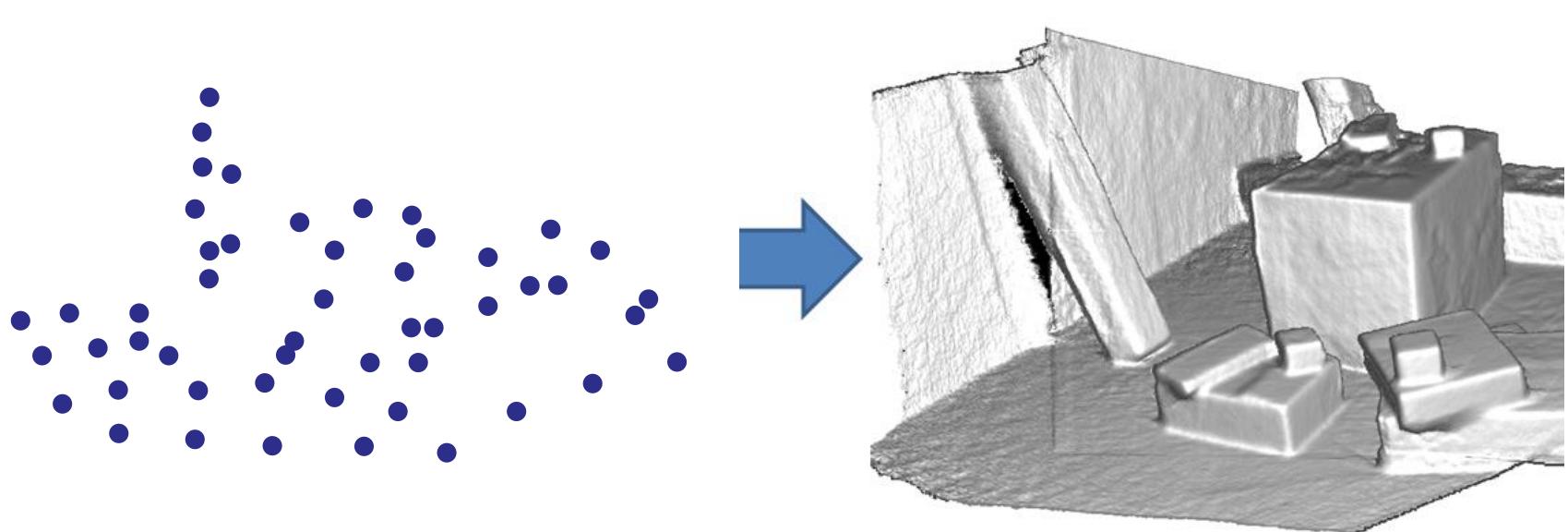
Parrot *senseFly*

Albris drone



5 vision sensors

# From Sparse to Dense 3D Models



# Dense Reconstruction Pipeline

## ➤ Local methods

- Estimate depth for every pixel independently using **photometric cost aggregation**

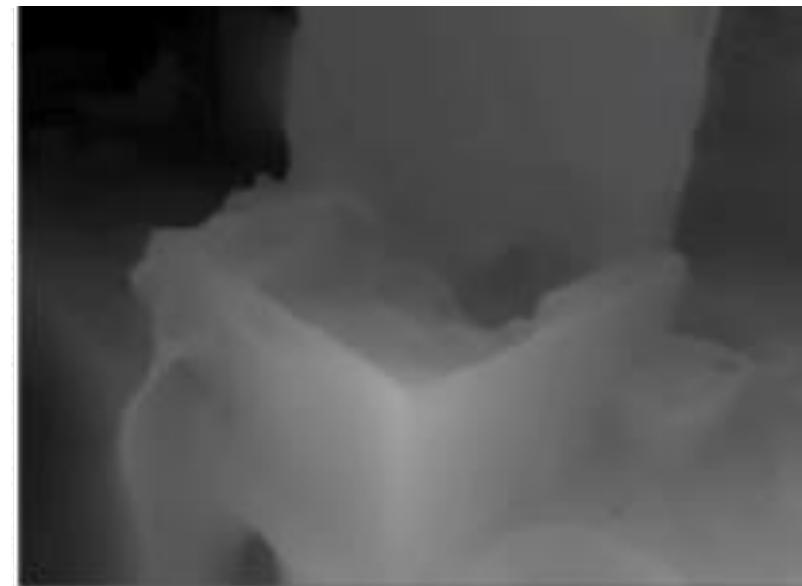
## ➤ Global methods

- Refine the depth surface as a whole by enforcing smoothness constraint  
("Regularization")

$$E(d) = E_d(d) + \lambda E_s(d)$$



Data termRegularization term:  
penalizes *non-smooth*  
surfaces

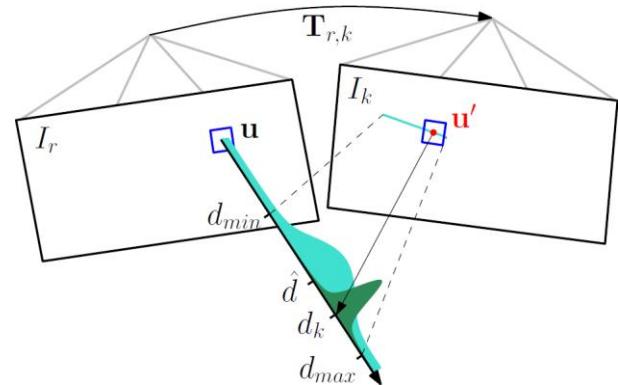


[Newcombe et al. 2011]

# REMODE: Probabilistic Monocular Dense Reconstruction [ICRA'14]

- Track independently every pixel using the same recursive Bayesian depth estimation of SVO

$$p(\tilde{d}_i^k | d_i, \rho_i) = \rho_i \mathcal{N}(\tilde{d}_i^k | d_i, \tau_i^2) + (1 - \rho_i) \mathcal{U}(\tilde{d}_i^k | d_i^{\min}, d_i^{\max})$$

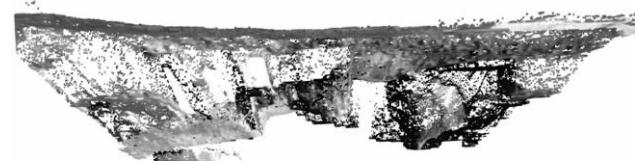


- A *regularized depth map*  $F(\mathbf{u})$  is computed from the noisy depth map  $D(\mathbf{u})$  as

$$\min_F \int_{\Omega} \{ G(\mathbf{u}) \|\nabla F(\mathbf{u})\|_{\epsilon} + \lambda \|F(\mathbf{u}) - D(\mathbf{u})\|_1 \} d\mathbf{u}$$



where  $G(\mathbf{u}) = \mathbb{E}_{\rho}[q](\mathbf{u}) \frac{\sigma^2(\mathbf{u})}{\sigma_{\max}^2} + \{1 - \mathbb{E}_{\rho}[q](\mathbf{u})\}$



Minimization is done using [Chambolle & Pock, 2011]

# REMODE: Probabilistic Monocular Dense Reconstruction [ICRA'14]

<https://www.youtube.com/watch?v=QTKd5UWCG0Q>

Running at 50 Hz on GPU on a Lenovo W530, i7



Monocular dense reconstruction  
in real-time from a hand-held camera

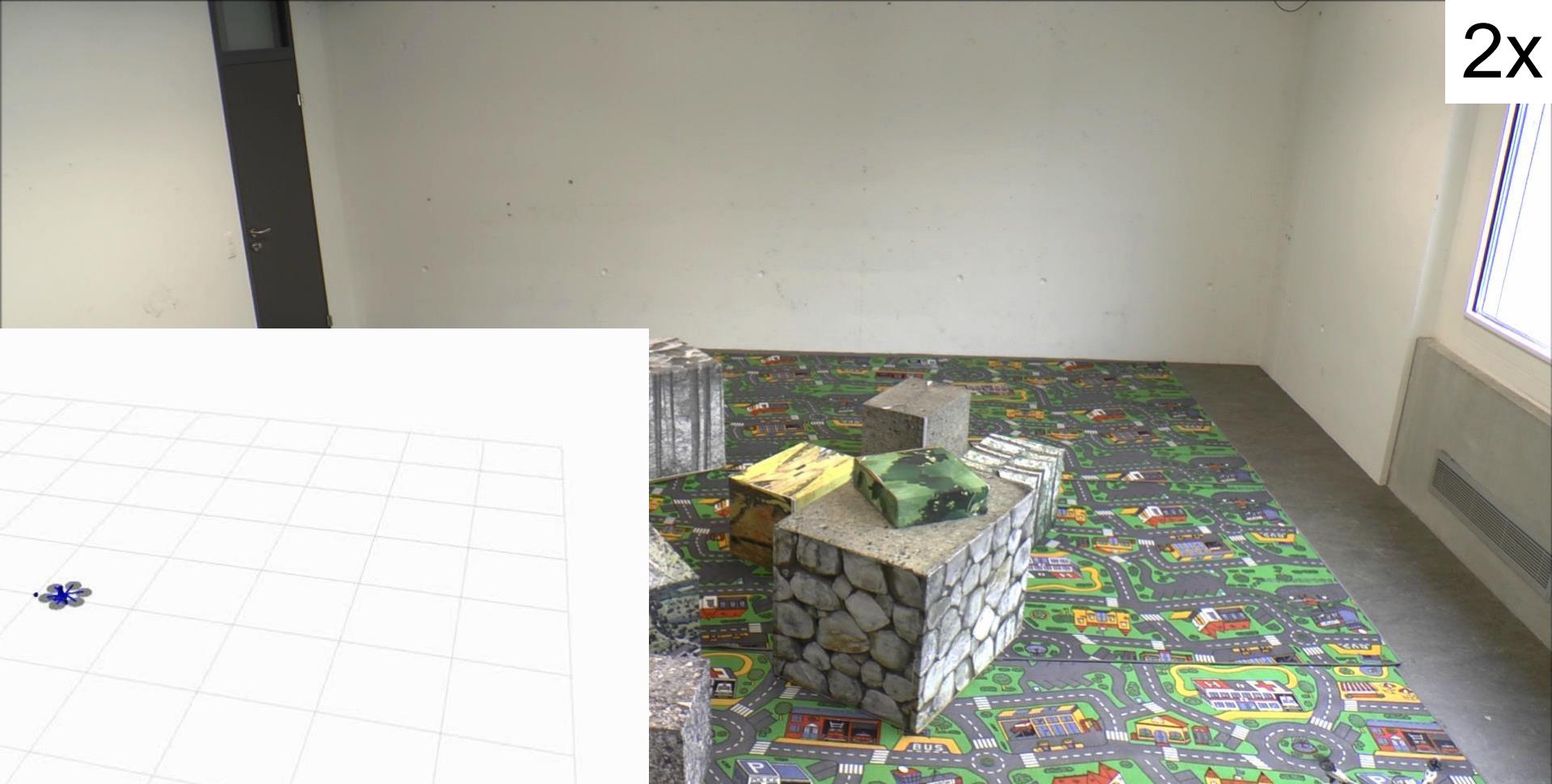
Open Source

Dataset from Gruber et al., "The City of Sights", ISMAR'10.

# Autonomus, Flying 3D Scanning

<https://www.youtube.com/watch?v=7-kPiWaFYAc>

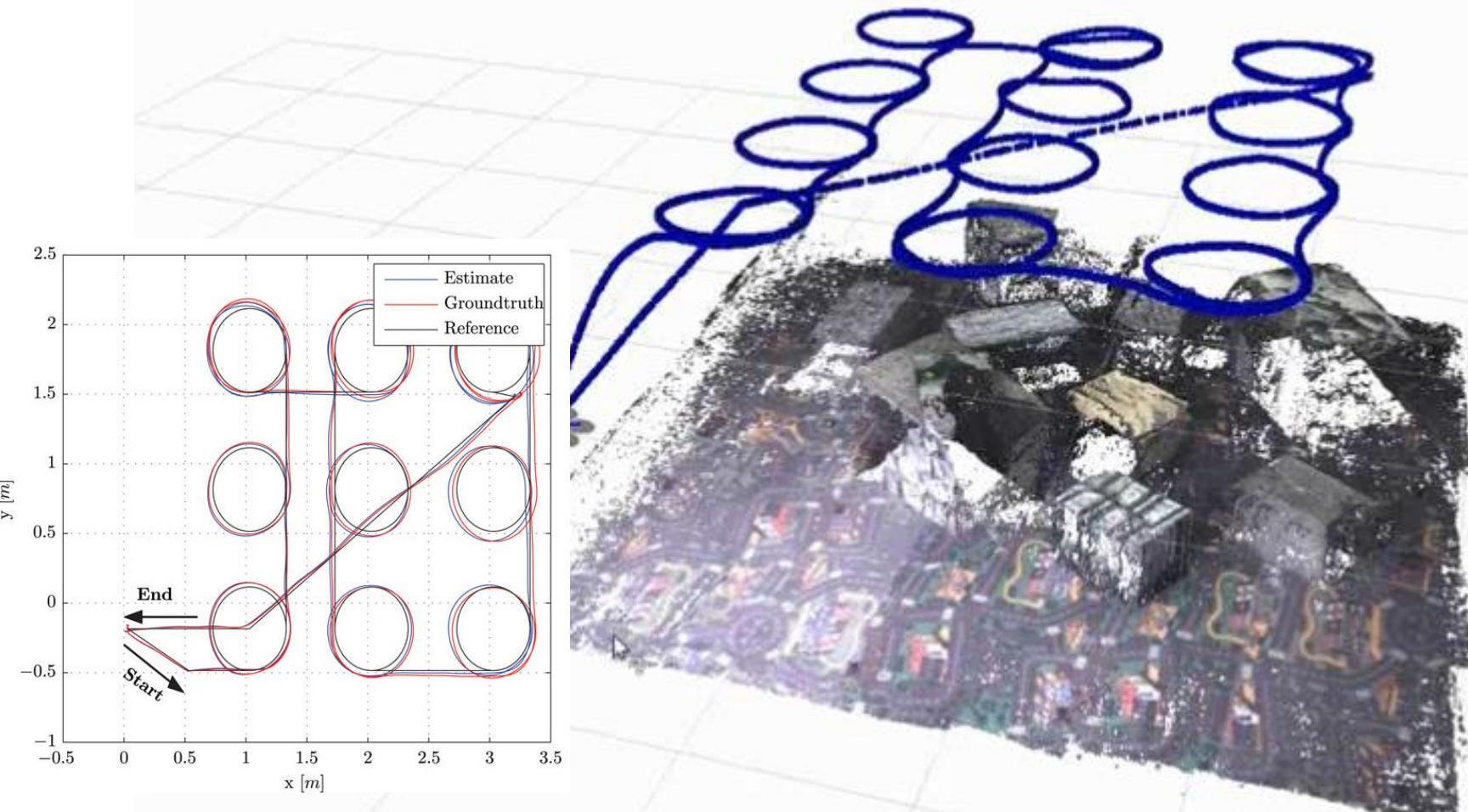
- Sensing, control, state estimation run onboard at 50 Hz (Odroid U3, ARM Cortex A9)
- Dense reconstruction runs live on video streamed to laptop (Lenovo W530, i7)



# Autonomus, Flying 3D Scanning [ JFR'15]

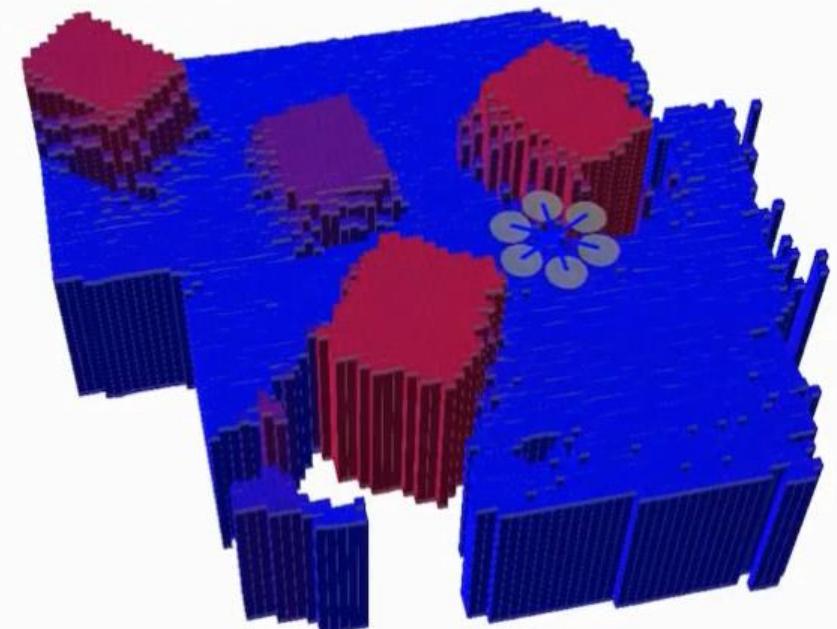
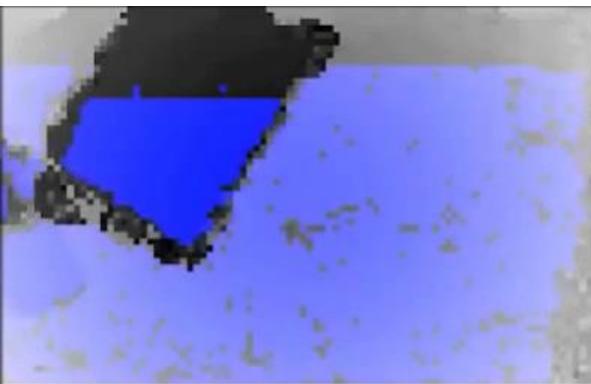
<https://www.youtube.com/watch?v=7-kPiWaFYAc>

- Sensing, control, state estimation run onboard at 50 Hz (Odroid U3, ARM Cortex A9)
- Dense reconstruction runs live on video streamed to laptop (Lenovo W530, i7)



# Autonomous Landing-Spot Detection and Landing

<https://www.youtube.com/watch?v=phaBKFwfcJ4>



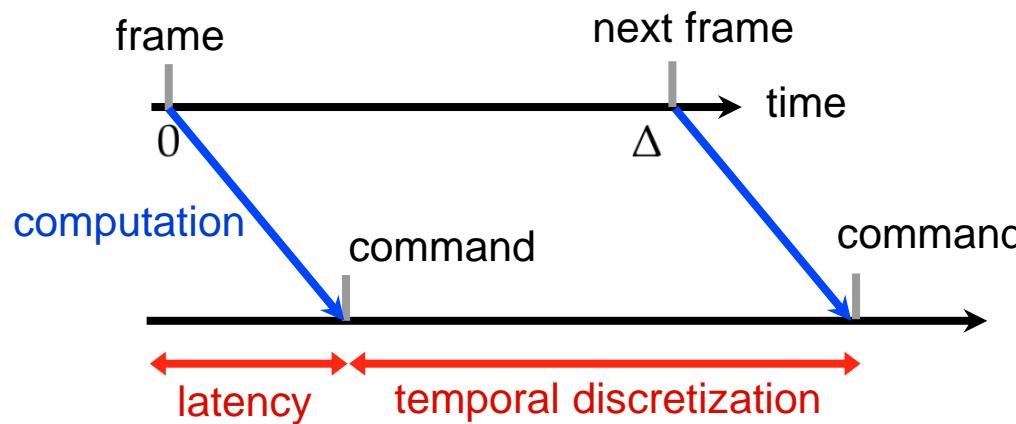
2x

# Outlook



# To go faster, we need faster sensors!

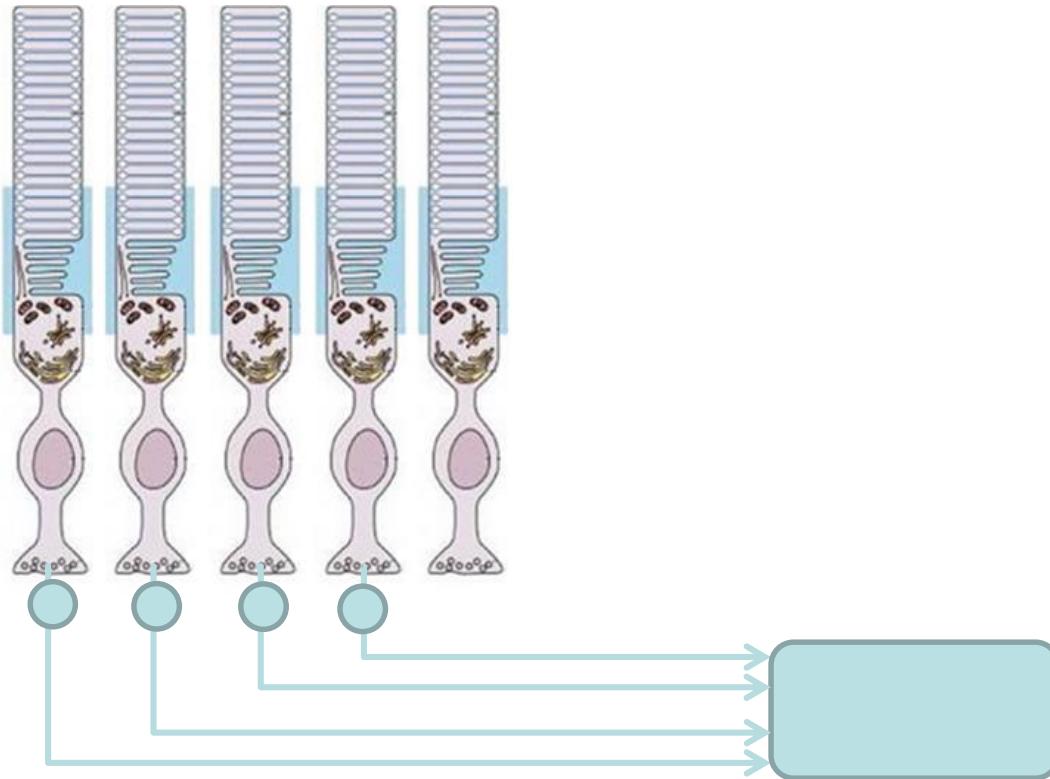
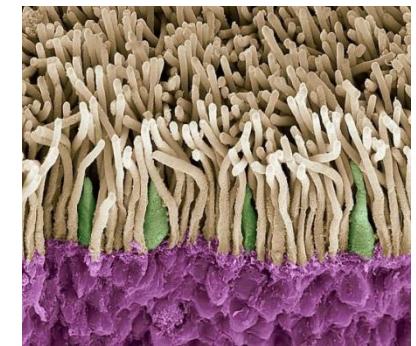
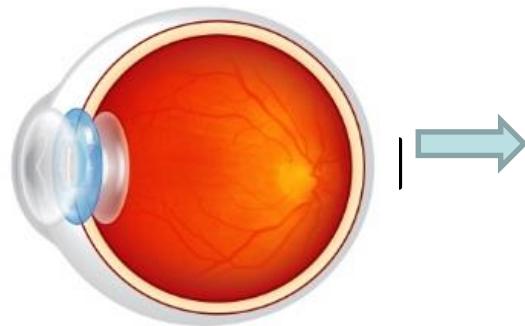
- At the current state, the agility of a robot is limited by the latency and temporal discretization of its sensing pipeline.
- Currently, the average robot-vision algorithms have latencies of 50-200 ms. This puts a hard bound on the agility of the platform.



- **Can we create a low-latency, low-discretization perception pipeline?**
  - Yes, if we use **event-based cameras**

# Human Vision System

- 130 million **photoreceptors**
- But only 2 million **axons**!



# Dynamic Vision Sensor (DVS)

- **Event-based camera** developed by Tobi Delbruck's group (ETH & UZH).
- Temporal resolution: **1  $\mu$ s**
- High dynamic range: **120 dB**
- Low power: **20 mW**
- Cost: 2,500 EUR

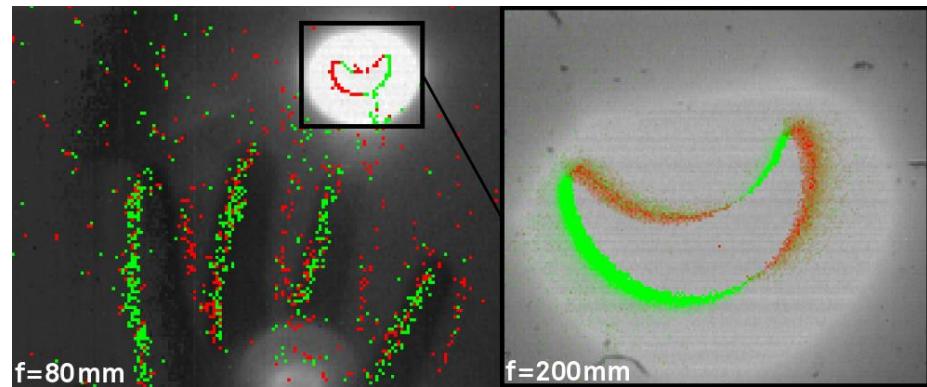
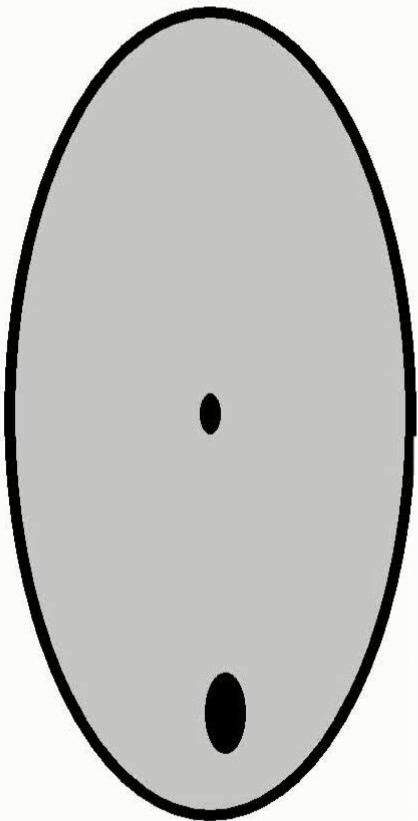


Image of the solar eclipse (March'15) captured by a DVS (courtesy of InILabs)

[Lichtsteiner, Posch, Delbruck. A 128x128 120 dB 15 $\mu$ s Latency Asynchronous Temporal Contrast Vision Sensor. 2008]

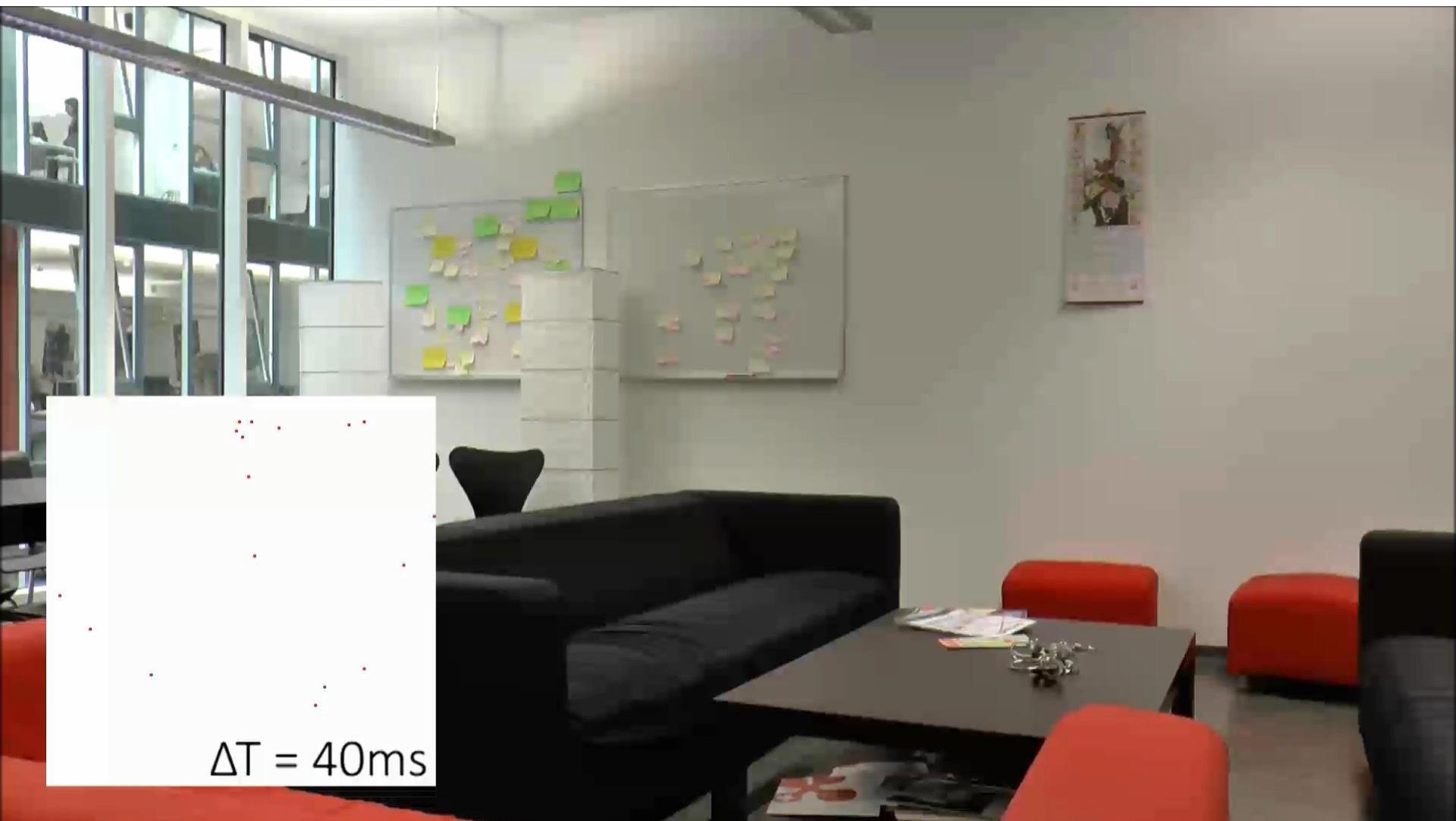
# Camera vs Dynamic Vision Sensor



**standard  
camera  
output:**



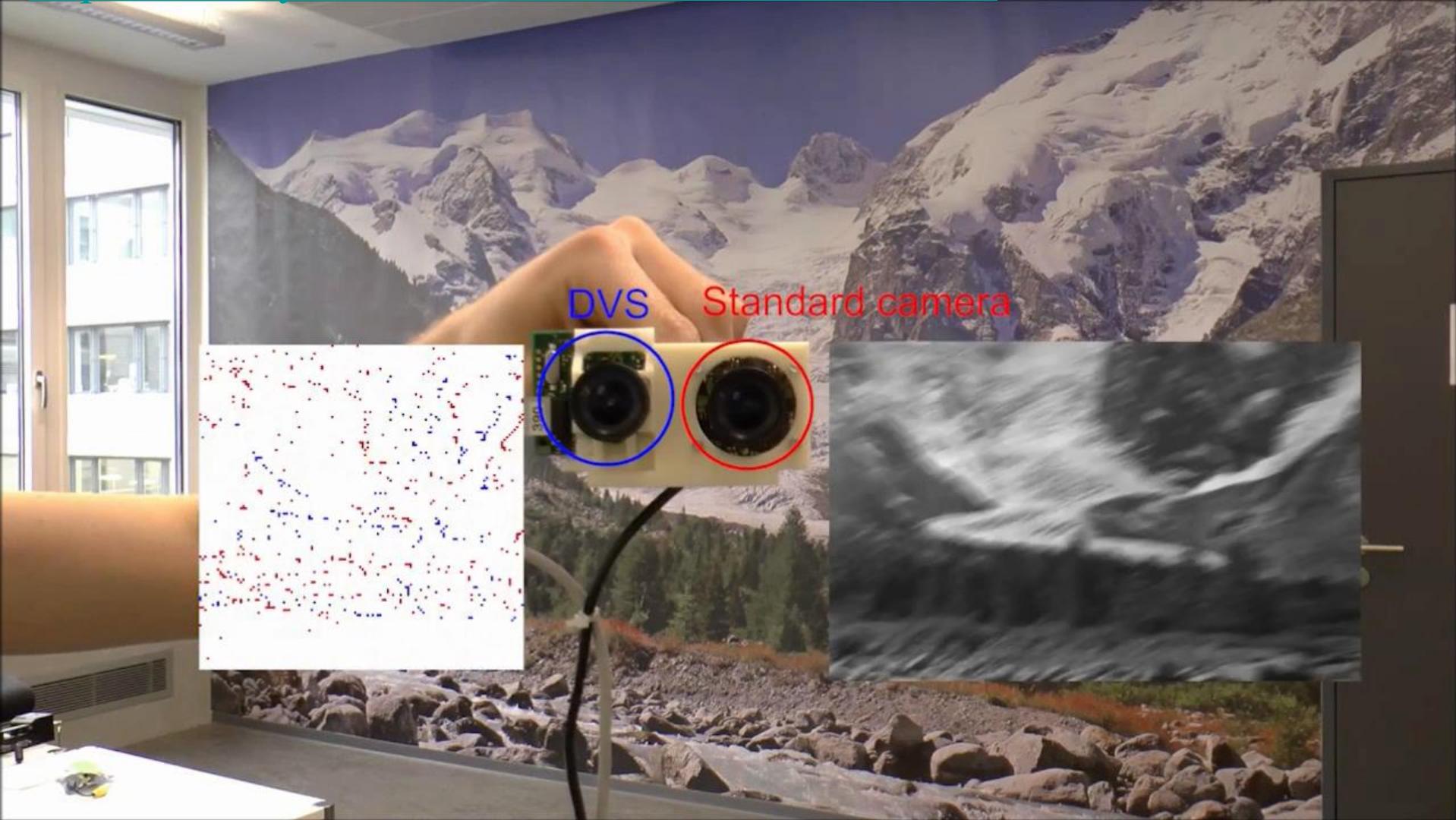
# Camera vs Dynamic Vision Sensor



<https://www.youtube.com/watch?v=LauQ6LWTkxM>

# High-speed State Estimation

<https://www.youtube.com/watch?v=iZZ77F-hwzs>



[Event-based Camera Pose Tracking using a Generative Event Model, Under review. Available at arXiv]

[Censi & Scaramuzza, *Low Latency, Event-based Visual Odometry*, ICRA'14]

# Conclusions

- Visual-inertial state estimation is crucial for GPS-denied navigation.
- More accurate than GPS, DGPS, and RTK-GPS.
- Pending challenges: robustness to changing illumination and high-speed motion.
- Event cameras are revolutionary visual sensors that can address such challenges where standard cameras fail.